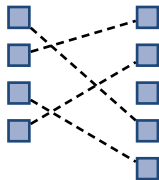
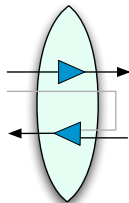


# Matching Lenses

Davi M. J. Barbosa (Polytechnique)  
Julien Cretin (Polytechnique/INRIA)  
Nate Foster (Cornell)  
Michael Greenberg (Penn)  
Benjamin C. Pierce (Penn)



# Example

---

=History (5 pts)=

List the inventors of the following programming languages.

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)

=Scoping (2 pts)=

Which of these terms are closed?

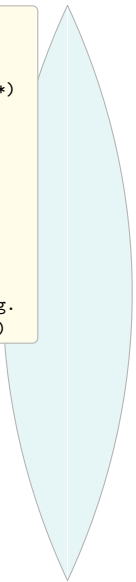
\*  $\lambda x.\lambda y.x$  (\* Yes \*)

\*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$  (\* No \*)

=Lambda Calculus (3 pts)=

Give a weakly normalizing term which is not strongly normalizing.

(\*  $(\lambda x.\lambda y.y) ((\lambda x.x x) \lambda x.x x)$  \*)



# Example

=History (5 pts)=

List the inventors of the following programming languages.

- \* Haskell 98 (\* Hudak,PJ,Wadler \*)
- \* LISP 58 (\* McCarthy \*)
- \* ML 73 (\* Gordon,Milner \*)

=Scoping (2 pts)=

Which of these terms are closed?

- \*  $\lambda x.\lambda y.x$  (\* Yes \*)
- \*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$  (\* No \*)

=Lambda Calculus (3 pts)=

Give a weakly normalizing term which is not strongly normalizing.

- (\*  $(\lambda x.\lambda y.y) ((\lambda x.x x) \lambda x.x x)$  \*)

=History=

List the inventors of the following programming languages.

- \* Haskell 98
- \* LISP 58
- \* ML 73

=Scoping=

Which of these terms are closed?

- \*  $\lambda x.\lambda y.x$
- \*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$

=Lambda Calculus=

Give a weakly normalizing term which is not strongly normalizing.

# Example

```
=History (5 pts)=  
List the inventors of the  
following programming languages.  
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)  
=Scoping (2 pts)=  
Which of these terms are closed?  
*  $\lambda x.\lambda y.x$  (* Yes *)  
*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$  (* No *)  
=Lambda Calculus (3 pts)=  
Give a weakly normalizing term  
which is not strongly normalizing.  
(*  $(\lambda x.\lambda y.y) ((\lambda x.x) \lambda x.x)$  *)
```

```
=History=  
List the inventors of the  
following programming languages.  
* Haskell 98  
* LISP 58  
* ML 73  
* OCaml 87  
* Haskell 90  
=Combinators=  
Give the equations for S and K in  
a combinatory algebra.  
=Scoping=  
Which of these terms are closed?  
*  $\lambda x.\lambda y.x$   
*  $\lambda x.(\lambda y.y) y$   
*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$   
=Lambda Calculus=  
Give a weakly normalizing term  
which is not strongly normalizing.
```

# Example

```
=History (5 pts)=  
List the inventors of the  
following programming languages.  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)  
* OCaml 87 (* TODO: answer *)  
* Haskell 90 (* Hudak,PJ,Wadler *)  
=Combinators (? pts)=  
Give the equations for S and K in  
a combinatory algebra.  
(* TODO: write the answer *)  
=Scoping (2 pts)=  
Which of these terms are closed?  
*  $\lambda x.\lambda y.x$  (* Yes *)  
*  $\lambda x.(\lambda y.y) y$  (* TODO: answer *)  
*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$  (* No *)  
=Lambda Calculus (3 pts)=  
Give a weakly normalizing term  
which is not strongly normalizing.  
(*  $(\lambda x.\lambda y.y) ((\lambda x.x x) \lambda x.x x)$  *)
```

```
=History=  
List the inventors of the  
following programming languages.  
* LISP 58  
* ML 73  
* OCaml 87  
* Haskell 90  
=Combinators=  
Give the equations for S and K in  
a combinatory algebra.  
=Scoping=  
Which of these terms are closed?  
*  $\lambda x.\lambda y.x$   
*  $\lambda x.(\lambda y.y) y$   
*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$   
=Lambda Calculus=  
Give a weakly normalizing term  
which is not strongly normalizing.
```

# Example

```
=History (5 pts)=  
List the inventors of the  
following programming languages.  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)  
* OCaml 87 (* TODO: answer *)  
* Haskell 90 (* Hudak,PJ,Wadler *)
```

```
=Combinators (? pts)
```

```
Give the equations for  
a combinatory algebra  
(* TODO: write the equations *)
```

```
=Scoping (2 pts)=
```

```
Which of these terms are closed?
```

```
*  $\lambda x.\lambda y.x$  (* Yes *)  
*  $\lambda x.(\lambda y.y) y$  (* TODO: answer *)  
*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$  (* No *)
```

```
=Lambda Calculus (3 pts)=
```

```
Give a weakly normalizing term  
which is not strongly normalizing.  
(*  $(\lambda x.\lambda y.y) ((\lambda x.x x) \lambda x.x x)$  *)
```

```
=History=
```

```
List the inventors of the  
following programming languages.  
* LISP 58  
* ML 73  
* OCaml 87  
* Haskell 90
```

```
=History (5 pts)=
```

```
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)
```

```
which of these terms are closed?
```

```
*  $\lambda x.\lambda y.x$   
*  $\lambda x.(\lambda y.y) y$   
*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$ 
```

```
=Lambda Calculus=
```

```
Give a weakly normalizing term  
which is not strongly normalizing.
```

## Basic lens with complement

---

A lens  $l$  is between a source set  $S$  and a view set  $V$ , and over a complement set  $C$ .

Notation:  $l \in S \overset{C}{\longleftrightarrow} V$

# Basic lens with complement

---

A lens  $l$  is between a source set  $S$  and a view set  $V$ , and over a complement set  $C$ .

Notation:  $l \in S \overset{C}{\longleftrightarrow} V$

The source  $S$  contains all the information (the full exam).

```
=History (5 pts)=  
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)
```



## Basic lens with complement

---

A **lens**  $l$  is between a source set  $S$  and a view set  $V$ , and over a complement set  $C$ .

Notation:  $l \in S \overset{C}{\longleftrightarrow} V$

The **view**  $V$  has **less** information than the source (we don't show the answers and number of points).

```
=History=  
* Haskell 98  
* LISP 58  
* ML 73
```

## Basic lens with complement

---

A *lens*  $l$  is between a source set  $S$  and a view set  $V$ , and over a complement set  $C$ .

Notation:  $l \in S \overset{C}{\longleftrightarrow} V$

The *complement*  $C$  represents the *missing* information (the answers and number of points).

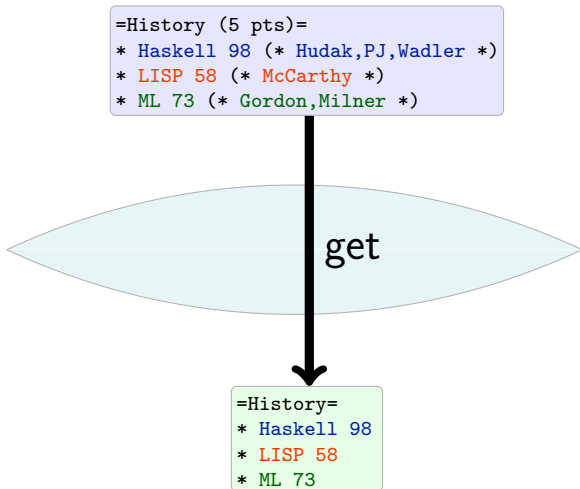
5 pts

Hudak, PJ, Wadler  
McCarthy  
Gordon, Milner

# Basic lens with complement

---

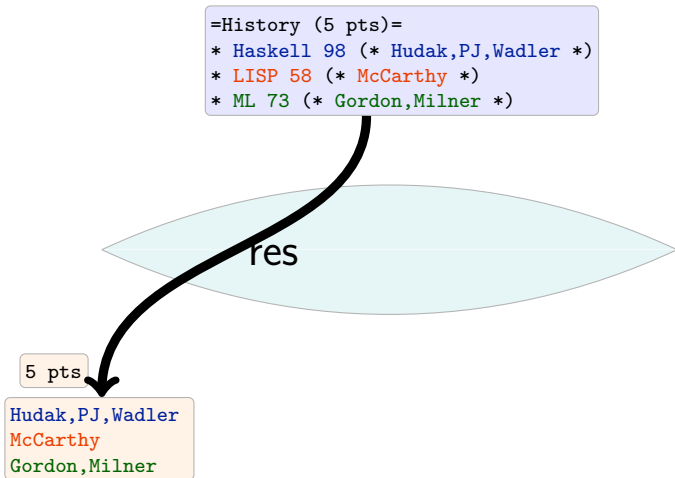
A lens comes with **three functions**: `get`,



# Basic lens with complement

---

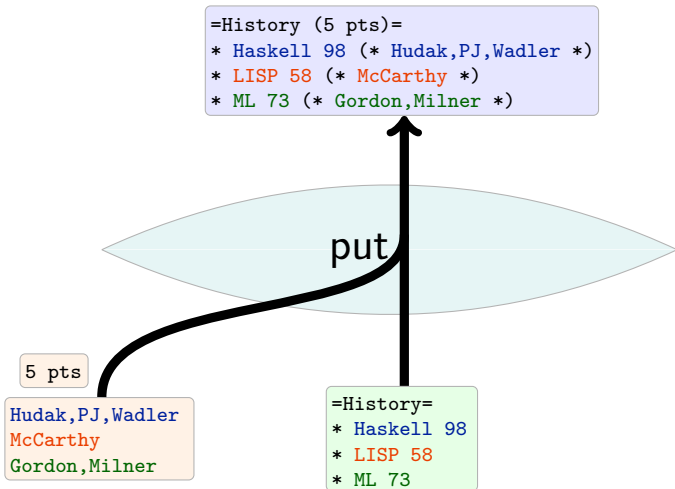
A lens comes with **three functions**: `get`, `res`



# Basic lens with complement

---

A lens comes with **three functions**: get, res and put.



## Basic lens with complement

---

$$l.get \in S \rightarrow V$$

$$l.res \in S \rightarrow C$$

$$l.put \in V \rightarrow C \rightarrow S$$

These functions obey **two round-tripping laws**, explaining the interoperation between `get`, `res` and `put`.

$$l.get (l.put v c) = v \quad (\text{PUTGET})$$

$$l.put (l.get s) (l.res s) = s \quad (\text{GETPUT})$$

# The alignment problem

---

```
=History (5 pts)=  
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)
```



# The alignment problem

---

```
=History (5 pts)=  
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)
```



get

```
=History=  
* Haskell 98  
* LISP 58  
* ML 73
```



# The alignment problem

---

```
=History (5 pts)=  
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)
```

get



```
=History=  
* Haskell 98  
* LISP 58  
* ML 73
```

edit

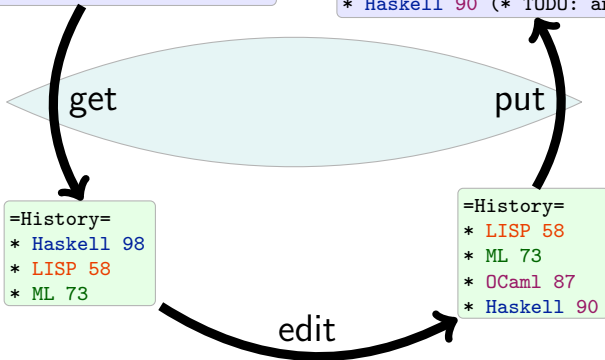
```
=History=  
* LISP 58  
* ML 73  
* OCaml 87  
* Haskell 90
```

# The alignment problem

---

```
=History (5 pts)=  
* Haskell 98 (* Hudak,PJ,Wadler *)  
* LISP 58 (* McCarthy *)  
* ML 73 (* Gordon,Milner *)
```

```
=History (5 pts)=  
* LISP 58 (* Hudak,PJ,Wadler *)  
* ML 73 (* McCarthy *)  
* OCaml 87 (* Gordon,Milner *)  
* Haskell 90 (* TODO: answer *)
```



# Challenges

---

- ▶ This problem is fundamentally heuristic
  - ▶ “state-based” lens only sees the result of edit
  - ▶ user intent must be inferred
- ▶ Appropriate heuristic depends on the application
- ▶ How to fit these heuristic behaviors into our principled lens framework?
  - ▶ how to formulate clean semantic laws involving “user intent”?

*[No previous work fully solves this problem.]*

# Matching Lenses

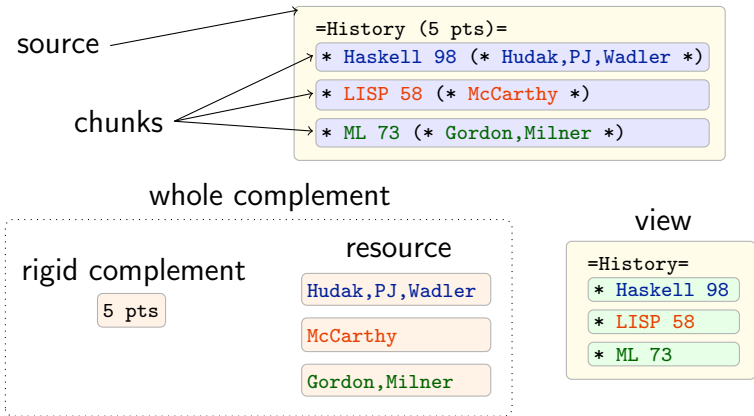
---

Goals:

- ▶ General solution (applicable to many heuristics)
- ▶ Clean theory (core laws parametrized on heuristics)

# Structures with chunks

In order to express the behavior of the put function in presence of view edits, we need to add structure to the source, view and complement types.



# Plan

---

- ▶ Start with something simple
  - ▶ *get* does not permute the items
  - ▶ items are not nested
  - ▶ only one sublen is used for all items
- ▶ Understand it fully
- ▶ Relax these simplifications

# Simple matching lenses

# Mechanism

---

=History (5 pts)=

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)





# Mechanism

---

=History (5 pts)=

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)

get



=History=

\* Haskell 98

\* LISP 58

\* ML 73

# Mechanism

---

=History (5 pts)=

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)

res



5 pts

Hudak,PJ,Wadler

McCarthy

Gordon,Milner

=History=

\* Haskell 98

\* LISP 58

\* ML 73

# Mechanism

---

=History (5 pts)=

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)

edit



5 pts

Hudak,PJ,Wadler

McCarthy

Gordon,Milner

=History=

\* Haskell 98

\* LISP 58

\* ML 73

=History=

\* LISP 58

\* ML 73

\* OCaml 87

\* Haskell 90

# Mechanism

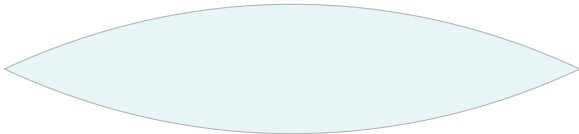
---

=History (5 pts)=

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)



5 pts

Hudak,PJ,Wadler

McCarthy

Gordon,Milner

=History=

\* Haskell 98

\* LISP 58

\* ML 73

=History=

\* LISP 58

\* ML 73

\* OCaml 87

\* Haskell 90

align (heuristic)

# Mechanism

=History (5 pts)=

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)



5 pts

Hudak,PJ,Wadler

McCarthy

Gordon,Milner

=History=

\* Haskell 98

\* LISP 58

\* ML 73

=History=

\* LISP 58

\* ML 73

\* OCaml 87

\* Haskell 90

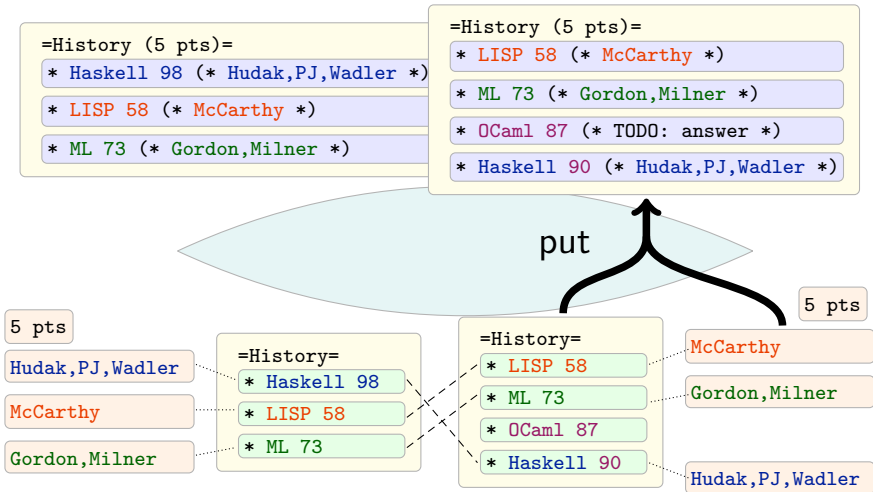
5 pts

McCarthy

Gordon,Milner

Hudak,PJ,Wadler

# Mechanism



# Matching lenses

---

A *matching lens*  $l$  is between  $S$  and  $V$ , and over a *rigid* complement  $C$  and a basic lens  $k$ .

We split the complement in two parts: a rigid complement  $C$ , and a resource (reorderable part)  $\{|\mathbb{N} \mapsto C_k|\}$ .

$$l.get \in S \rightarrow V$$

$$l.res \in S \rightarrow \boxed{C \times \{|\mathbb{N} \mapsto C_k|\}}$$

whole complement

$$l.put \in V \rightarrow \boxed{C \times \{|\mathbb{N} \mapsto C_k|\}} \rightarrow S$$

# Matching lenses

---

A *matching lens*  $l$  is between  $S$  and  $V$ , and over a *rigid* complement  $C$  and a basic lens  $k$ .

We split the complement in two parts: a rigid complement  $C$ , and a resource (reorderable part)  $\{|\mathbb{N} \mapsto C_k|\}$ .

$$l.get \in S \rightarrow V$$

$$l.res \in S \rightarrow \boxed{C \times \{|\mathbb{N} \mapsto C_k|\}}$$

whole complement

$$l.put \in V \rightarrow \boxed{C \times \{|\mathbb{N} \mapsto C_k|\}} \rightarrow S$$

rigid complement



# Matching lenses

---

A *matching lens*  $l$  is between  $S$  and  $V$ , and over a *rigid* complement  $C$  and a basic lens  $k$ .

We split the complement in two parts: a rigid complement  $C$ , and a resource (reorderable part)  $\{|\mathbb{N} \mapsto C_k|\}$ .

$$l.get \in S \rightarrow V$$

$$l.res \in S \rightarrow \boxed{C \times \{|\mathbb{N} \mapsto C_k|\}}$$

whole complement

$$l.put \in V \rightarrow \boxed{C \times \{|\mathbb{N} \mapsto C_k|\}} \rightarrow S$$

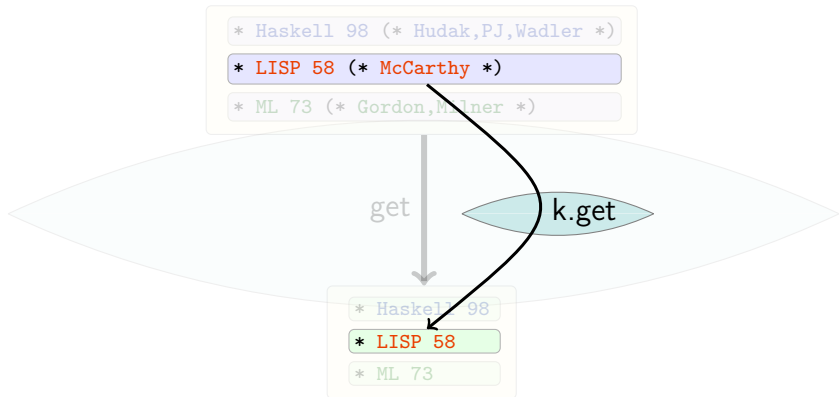
rigid complement

resource (reorderable part)

# ChunkGet

---

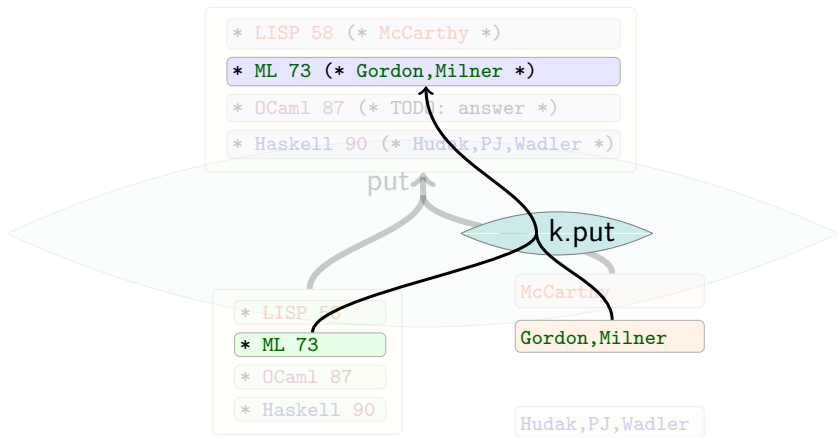
We add **new laws** guiding how the lens operate.



# ChunkPut

---

We add **new laws** guiding how the lens operate in presence of view edits.

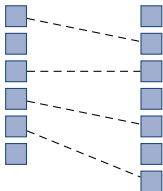


# Heuristics

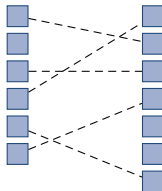
---

We can now get benefit of our framework, by considering several heuristics.

We have implemented heuristics that minimize a cost function on an alignment search space.



diffy



setlike

# Syntax of the example

---

```
module Example =

let field (b:bool) =
  let c = [A-Za-z0-9():,.?] | "" in
  let w =
    match b with
    | true -> [ \n ]
    | false -> ' '
  :regexp
  in ( c | c . (c | w)* . c )

let topic =
  copy ("=" . field false)
  . default
    (del (" (" . [?1-9] . " pts"))
      " (? pts)")
  . copy "\n"

let question =
  copy ("* " . field false)
  . default
    (del (" (* " . field false . " *"))
      " (* TODO: answer *)")
  . copy "\n"
```

```
let subject = field true . "\n"

let exercise1 =
  let q = setlike 0 "question" in
  topic . subject . <q:key question > +

let exercise2 =
  topic . subject
  . default
    (del ("(* " . field true . " *)\n"))
    "(* TODO: write the answer *)\n"

let main_lens =
  let e1 = setlike 0 "exercise1" in
  let e2 = setlike 0 "exercise2" in
  ( <e1:key ( align exercise1) >
    | <e2:key ( align exercise2) > )*
```

# Extensions

# Nested chunks

---

We can handle several levels of chunks.

=History (5 pts)=

List the inventors of the following programming languages.

\* Haskell 98 (\* Hudak,PJ,Wadler \*)

\* LISP 58 (\* McCarthy \*)

\* ML 73 (\* Gordon,Milner \*)

=Scoping (2 pts)=

Which of these terms are closed?

\*  $\lambda x.\lambda y.x$  (\* Yes \*)

\*  $(\lambda x.\lambda z.x) \lambda x.\lambda y.z$  (\* No \*)

=Lambda Calculus (3 pts)=

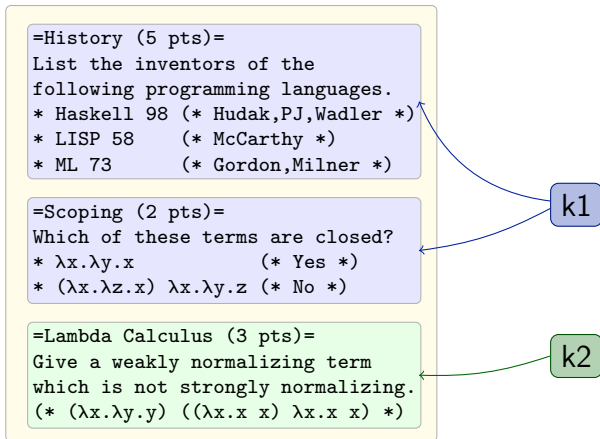
Give a weakly normalizing term which is not strongly normalizing.

(\*  $(\lambda x.\lambda y.y) ((\lambda x.x x) \lambda x.x x)$  \*)

# Tags

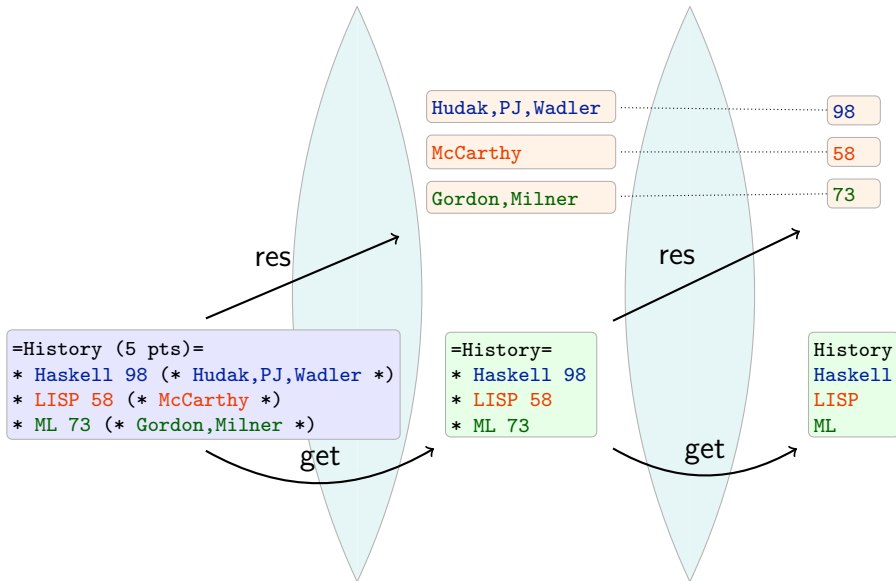
---

We can also have several kinds of chunks which are processed in different ways.





# Composition



# Related work

---

## Positional

- ▶ Focal — [TOPLAS '07]
- ▶ semantic bidirectionalization — [Vogtlaender '09]
- ▶ syntactic bidirectionalization — [Matsuda '07]
- ▶ point free lenses — [Pacheco and Cunha '10]

## Update-based

- ▶ most databases
- ▶ X and Inv — [Hu, Mu and Takeichi '04]
- ▶ constraint maintainers — [Merteens '98]
- ▶ u-lenses — [Diskin, Xiong and Czarnecki '10]

# Dictionary lenses

---

**Idea:** use keys for alignment [POPL '08]

**Mechanism:** build a dictionary, thread it through put

**Limitations:**

- ▶ we don't necessarily have keys,
- ▶ the update can change keys, and
- ▶ weird composition

**Benefits of matching lenses:**

- ▶ modularity
- ▶ enable use of global heuristics
- ▶ stronger semantic laws

# Conclusion

---

- ▶ The **alignment problem** was an often eluded and not well understood issue arising whenever we handle a list of items in a lossy way, which is the case in many applications.
- ▶ The notion of **chunks** allows to precisely tell which parts of the source are linked.
- ▶ **Abstracting the alignment** from the lens's work makes the distinction between them clear.
- ▶ The behavior of put with edits on the view is now specified in the semantic using **new laws**
- ▶ The lens theory still remains quite simple

# Thank You!

---

**Collaborators:** Davi Barbosa, Nate Foster, Michael Greenberg, Benjamin Pierce

**Boomerang contributors:** Aaron Bohannon, Martin Hofmann, Alexandre Pilkiewicz, Alan Schmitt, and Daniel Wagner.



**Want to play?** Boomerang is available for download:

- ▶ Source code (LGPL)
- ▶ Binaries for OS X, Linux
- ▶ Research papers
- ▶ Tutorial, manual and demos

<http://www.seas.upenn.edu/~harmony/>

Extra slides

## Matching lens laws (1/2)

---

$$locations(s) = locations(l.get\ s) \text{ (GETCHUNKS)}$$

$$\frac{c, r = l.res\ s}{locations(s) = \text{dom}(r)} \text{ (RESCHUNKS)}$$

$$\frac{n \in (locations(v) \cap \text{dom}(r))}{(l.put\ v\ (c, r))[n] = k.put\ v[n]\ (r(n))} \text{ (CHUNKPUT)}$$

$$\frac{n \in (locations(v) \setminus \text{dom}(r))}{(l.put\ v\ (c, r))[n] = k.create\ v[n]} \text{ (NOCHUNKPUT)}$$

$$\frac{skel(v) = skel(v')}{skel(l.put\ v\ (c, r)) = skel(l.put\ v'\ (c, r'))} \text{ (SKELPUT)}$$

## Matching lens laws (2/2)

---

$$l.get (l.create v r) = v \quad (\text{CREATEGET})$$

$$\frac{n \in (\text{locations}(v) \cap \text{dom}(r))}{(l.create v r)[n] = k.put v[n] (r(n))} \quad (\text{CHUNKCREATE})$$

$$\frac{n \in (\text{locations}(v) \setminus \text{dom}(r))}{(l.create v r)[n] = k.create v[n]} \quad (\text{NOCHUNKCREATE})$$

$$\frac{\text{skel}(v) = \text{skel}(v')}{\text{skel}(l.create v r) = \text{skel}(l.create v' r')} \quad (\text{SKELCREATE})$$

$$l.get (l.put v (c, r)) = v \quad (\text{PUTGET})$$

$$l.put (l.get s) (l.res s) = s \quad (\text{GETPUT})$$