Formally Verified Cryptographic Web Applications in WebAssembly

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May 6th 2019

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Examples of cryptographic applications beyond TLS

- Storing encrypted data on servers (Lastpass).
- End-to-end encryption between devices (Whatsapp, Signal).

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Web cryptographic solutions

- The WebCrypto API (fast, reliable, but only certain primitives)
- Custom Javascript (slow, not secure [BDLM14])
- asm.js (C compiled to Javascript)
- WebAssembly (new !)

Challenge : bringing verification to Web applications

Here is how Signal implements its cryptographic protocol:



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How do we get verified software inside this architecture?

Choosing the toolchain



Online toolchain: what is WebAssembly?

WebAssembly [Haa+17] is

- a low-level intermediate representation (or a macro-assembler);
- with structured control flow;
- written as an AST;
- architecture-independent;
- typechecked before execution;
- formally specified;
- memory-management-agnostic (it gives only a flat memory buffer);
- modular with a simple import-export semantic;
- interoperable with Javascript.

A WebAssembly function

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```
(module
(export "fib" (func $fib))
(func $fib (param $n i32) (result i32)
 (if (i32.lt_s
   (get_local $n)
   (i32.const 2))
   (return (i32.const 1))
  (return (i32.add
   (call $fib (i32.sub (get_local $n) (i32.const 2)))
   (call $fib (i32.sub (get local $n) (i32.const 1)))
  ))
```

Building a toolchain on top of WebAssembly

WebAssembly is better suited to cryptographic software than Javascript (machine arithmetic, manual memory management). It is the second best choice after using the WebCrypto API.

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Problem

- Should we translate C to WebAssembly?
- Or directly from Low* to WebAssembly?

The case for a domain-specific compiler to WebAssembly

Going via Clight

- + Reusing existing toolchains (Low* to Clight and Emscripten)
- No verified translation to WebAssembly (unless it's added to CompCert...)
- $-\,$ Formalization has to deal with C99 scopes and other C details
- Loss of information (e.g. immutable local variables)

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Custom intermediate language C \flat

- $-\,$ Have to fork the existing Low* toolchain
- $+\ C\flat$ is expression-based, no undefined behaviour
- + Simpler to formalize
- $\ + \ Custom, \ stack-based \ memory \ management$

From F* to WebAssembly



F* specification, Low* implementation

F*

```
let prime = pow2 255 - 19
type elem = e:int{e >= 0 /\ e < prime}
let add e1 e2 = (e1 + e2) % prime
let mul e1 e2 = (e1 * e2) % prime
let zero: elem = 0
let one: elem = 1</pre>
```

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I ow*
type felem = p:uint64 p { length p = 5 }
let fadd (output a b: felem): Stack unit
  (requires (fun h0 -> live pointers h0 [output; a; b] /
    fadd_pre h0.[a] h0.[b])
  (ensures (fun h0 h1 -> modifies only output h0 h1 /\
    h1.[output] == add h0.[a] h0.[b]))
                                                     ▲□▶ ▲課▶ ★注▶ ★注▶ 注: のへぐ
```

λow^* and Cb syntax

$$\tau ::= \operatorname{int} 32 | \operatorname{int} 64 | \operatorname{unit} | \{\overline{f} = \tau\} | \operatorname{buf} \tau | \alpha$$

$$v ::= x | g | k : \tau | () | \{\overline{f} = v\}$$

$$e ::= \operatorname{readbuf} e_1 e_2 | \operatorname{writebuf} e_1 e_2 e_3 | \operatorname{newbuf} n (e_1 : \tau)$$

$$| \operatorname{subbuf} e_1 e_2 | e.f | v | \operatorname{if} e_1 \operatorname{then} e_2 \operatorname{else} e_3$$

$$| d \overrightarrow{e} | \operatorname{let} x : \tau = e_1 \operatorname{in} e_2 | \{\overline{f} = e\} | e \oplus n | \operatorname{for} i \in [0; n) e$$

$$P ::= \cdot | \operatorname{let} d = \lambda \overline{y} : \tau \cdot e_1 : \tau_1, P | \operatorname{let} g : \tau = e, P$$

$\lambda \mathsf{ow}^{\pmb{\ast}} \text{ and } \mathsf{C}\flat \text{ syntax}$

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$$P ::= \cdot | \operatorname{let} d = \lambda \overline{y : \tau} \cdot e_1 : \tau_1, P | \operatorname{let} g : \tau = e, P$$

$$\hat{\tau} ::= \operatorname{int} 32 | \operatorname{int} 64 | \operatorname{unit} | \operatorname{pointer}$$

$$\hat{v} ::= \ell | g | k : \hat{\tau} | ()$$

$$\hat{e} ::= \operatorname{read}_{n} \hat{e} | \operatorname{write}_{n} \hat{e}_{1} \hat{e}_{2} | \operatorname{new} \hat{e} | \hat{e}_{1} \oplus \hat{e}_{2} | \ell := \hat{e} | \hat{v} | \hat{e}_{1}; \hat{e}_{2}$$

$$| \operatorname{if} \hat{e}_{1} \operatorname{then} \hat{e}_{2} \operatorname{else} \hat{e}_{3} : \hat{\tau} | \operatorname{for} \ell \in [0; n) \hat{e} | \hat{e}_{1} \times \hat{e}_{2} | \hat{e}_{1} + \hat{e}_{2} | d \stackrel{\frown}{\hat{e}}$$

$$\hat{P} ::= \cdot | \operatorname{let} d = \lambda \overline{\ell : \hat{\tau} . \ell : \hat{\tau}}, \hat{e} : \hat{\tau}, \hat{P} | \operatorname{let} g : \hat{\tau} = \hat{e}, \hat{P}$$

λow^* to Cb: desugaring structure values

- let $d = \lambda v : \tau_1 . e : \tau_2$ let $d = \lambda v : \tau_1 \cdot e : \tau_2$
- $f(e:\tau)$ $(f e): \tau$
- let $x : \tau = e_1$ in e_2 $\{\overline{f = e}\}$ (not under newbuf)
- take addr(let $x : \tau = e_1$ in e_2) \rightarrow let $x : \tau = e_1$ in take addr e_2
- \rightarrow let $d = \lambda y$: buf τ_1 . [readbuf y 0/y] $e: \tau_2$ \rightarrow let $d = \lambda v : \tau_1 . \lambda r :$ buf τ_2 . let $x : \tau_2 = e$ in writebuf $r \mid 0 \mid x :$ unit \rightarrow let x : buf τ = newbuf 1 e in f x \rightarrow let x : buf τ = newbuf 1 (_ : τ) in f e x; readbuf x 0 \rightarrow let x : buf τ = take addr e_1 in [readbuf x 0/x] e_2 \rightarrow let x : buf $\{\overline{f=\tau}\}$ = newbuf 1 $\{\overline{f=e}\}$ in readbuf x 0 take_addr(readbuf e n) \rightsquigarrow subbuf e n take_addr($(e:\overline{f:\tau}).f$) \rightsquigarrow take_addr(e) \oplus offset($\overline{f:\tau},f$)
- take addr(if e_1 then e_2 else e_3) \rightarrow if e_1 then take addr e_2 else take addr e_3

λ ow* to C \flat : performing the struct layout

size int32 = 4 = 4 size unit size int64 = 8 size buf τ = 4 size $\overrightarrow{f:\tau}$ = offset $(\overrightarrow{f:\tau}, f_n)$ + size τ_n offset $(\overrightarrow{f:\tau}, f_0) = 0$ offset $(\overline{f:\tau}, f_{i+1})$ = align(offset $(\overline{f:\tau}, f_i)$ + size τ_i , alignment τ_{i+1}) alignment($\overline{f:\tau}$) = 8 $\operatorname{alignment}(\tau) = \operatorname{size} \tau$ otherwise align(k, n) = k align(k, n) = k + n - (k mod n) if $k \mod n = 0$ otherwise

λow^* to Cb: some rules I

LET

$$G; V \vdash e_{1} : \tau_{1} \Rightarrow \hat{e}_{1} : \hat{\tau}_{1} \dashv V'$$

$$\frac{\ell \text{ fresh}}{G; (x \mapsto \ell, \hat{\tau}_{1}) \cdot V' \vdash e_{2} : \tau_{2} \Rightarrow \hat{e}_{2} : \hat{\tau}_{2} \dashv V''}$$

$$\overline{G; V \vdash \text{ let } x : \tau_{1} = e_{1} \text{ in } e_{2} : \tau_{2} \Rightarrow \ell := \hat{e}_{1}; \hat{e}_{2} : \hat{\tau}_{2} \dashv V''}$$

$$\frac{G}{G}; \overrightarrow{y \mapsto \ell, \hat{\tau}} \vdash e_{1} : \tau_{1} \Rightarrow \hat{e}_{1} : \hat{\tau}_{1} \dashv \overrightarrow{x \mapsto \ell', \hat{\tau}'} \cdot \overrightarrow{y \mapsto \ell, \hat{\tau}} = V_{AR} \quad V(x) = \ell, \tau \quad V_{AR} \quad V_{AR}$$

BUFWRITE

$$G; V \vdash \text{writeB} (e_1 + e_2 \times \text{size } \tau_1) e_3 \Rightarrow \hat{e} \dashv V'$$

$$\overline{G; V \vdash \text{writebuf} (e_1 : \tau_1) e_2 e_3} \Rightarrow \hat{e} : \text{unit} \dashv V'$$

λ ow* to Cb: some rules II

$$\frac{W_{\text{RITEINT}32}}{G; V \vdash e_1 \Rightarrow \hat{e}_1 \dashv V'} \quad G; V' \vdash e_2 \Rightarrow \hat{e}_2 \dashv V''} \frac{G; V \vdash e_1 \Rightarrow \hat{e}_1 \dashv V'}{G; V \vdash \text{writeB } e_1 (e_2 : \text{int}32) \Rightarrow \text{write}_4 \hat{e}_1 \hat{e}_2 \dashv V''}$$

WRITELITERAL

$$\frac{G; V_i \vdash \text{writeB} (e + \text{offset} (\overline{f:\tau}, f_i)) e_i \Rightarrow \hat{e}_i \dashv V_{i+1}}{G; V_0 \vdash \text{writeB} e (\{\overline{f=e:\tau}\}) \Rightarrow \hat{e}_0; \dots; \hat{e}_{n-1} \dashv V_n}$$

WRITEDEREF ℓ fresh $V' = \ell$, int $32 \cdot V$ $G; V \vdash v_i \Rightarrow \hat{v}_i \dashv V$ memcpy $v_1 v_2 n =$ for $\ell \in [0; n)$ write₁ $(v_1 + \ell)$ (read₁ $(v_2 + \ell)$ 1) $\overline{G; V \vdash \text{writeB } v_1 \text{ (readbuf } (v_2 : \tau_2) 0) \Rightarrow \text{memcpy } v_1 v_2 \text{ (size } \tau_2) \dashv V'}$

λ ow* to C \flat : some rules III



Cb to WebAssembly: memory management helpers

We adopt a stack-based memory allocation scheme with a watermark at address 0.

$C\flat$ to WebAssembly: some rules I

$\mathsf{C}\flat$ to WebAssembly: some rules II

Func

$$\hat{\mathbf{e}} \Rightarrow \overrightarrow{i} \qquad \hat{\tau}_i \Rightarrow t_i$$

$$\boxed{\mathsf{let } d = \lambda \overline{\ell_1} : \hat{\tau_1} . \overline{\ell_2} : \hat{\tau}_2, \hat{\mathbf{e}} : \hat{\tau} \Rightarrow} \\ d = \mathsf{func } \overrightarrow{t_1} \rightarrow t \mathsf{ local } \overline{\ell_1} : t_1 \cdot \ell_2 : t_2 \cdot \ell : t. \\ \mathsf{call get_stack; } \overrightarrow{i} ; \mathsf{ store_local } \ell ; \mathsf{ call set_stack; get_local } \ell \end{aligned}$$

Example: compiled fadd function

```
fadd = func [int32; int32; int32] \rightarrow []
  local [\ell_0, \ell_1, \ell_2: int 32; \ell_3: int 32; \ell: int 32].
  call get stack: loop(
     // Push dst + 8*i on the stack
     get_local \ell_0; get_local \ell_3; i32.const 8; i32.binop*; i32.binop+
     // Load a + 8*i on the stack
     get local \ell_1; get local \ell_3; i32.const 8; i32.binop*; i32.binop+
     i64 load
     // Load b + 8*i on the stack (elided, same as above)
     // Add a.[i] and b.[i]. store into dst.[i]
     i64.binop+; i64.store
     // Per the rules. return unit
     i32.const 0; drop
     // Increment i; break if i == 5
     get local \ell_3; i32.const 1; i32.binop+; tee_local \ell_3
     i32.const 5; i32.op =; br if
   ): i32.const 0
  store local \ell : call set stack: get local \ell
```

The compiler, KreMLin, is 11,000 LOC. The translation is implemented following this formalization, and is designed to be auditable.

We left as future work the task of replicating and adapting the translation correctness of [Pro+17] from λow^* to Clight:

Lemma

Let *P* be a λow^* program and *e* be a λow^* entry point expression, and assume that they compile: $\downarrow \downarrow (P) = \hat{P}$ for some C^{*} program \hat{P} and $\downarrow (e) = \overrightarrow{s}$; \hat{e} for some C^{*} list of statements \overrightarrow{s} and expression \hat{e} .

Let V be a mapping of local variables containing the initial values of secrets. Then, the C^{*} program \hat{P} terminates with trace ℓ and return value v, i.e.,

 $\hat{P} \vdash ([], V, \vec{s}; \text{return } \hat{e}) \stackrel{\ell,*}{\rightarrow} ([], V', \text{return } v)$ if, and only if, so does the λow^* program: $P \vdash (\{\}, e[V]) \stackrel{\ell,*}{\rightarrow} (H', v);$ and similarly for divergence.

Future work: secret independence theorem

Theorem

From [Pro+17], proven for the translation from $\lambda \text{ow*}$ to Clight: given

- **1** a program well-typed against a secret interface, Γ_s , i.e, $\Gamma_s, \Gamma_P; \Sigma; \Gamma \vdash (H, e) : \tau$,
- 2 a well-typed implementation of the Γ_s interface, $\Gamma_s; \Sigma; \cdot \vdash_{\Delta} P_s$, such that P_s is equivalent modulo secrets,
- **3** a pair (ρ_1, ρ_2) of well-typed substitutions for Γ ,

then either:

- 1 both programs cannot reduce further, i.e. $P_s, P \vdash (H, e)[\rho_1] \Rightarrow \text{ and } P_s, P \vdash (H, e)[\rho_2] \Rightarrow$, or
- 2 both programs make progress with the same trace, i.e. there exists $\Sigma' \supseteq \Sigma, \Gamma' \supseteq \Gamma, H', e'$, a pair (ρ'_1, ρ'_2) of well-typed substitutions for Γ' , and a trace ℓ such that

i)
$$P_s, P \vdash (H, e)[\rho_1] \rightarrow_{\ell}^+ (H', e')[\rho'_1]$$
 and $P_s, P \vdash (H, e)[\rho_2] \rightarrow_{\ell}^+ (H', e')[\rho'_2]$, and
ii) $\Gamma_s, \Gamma_P; \Sigma'; \Gamma' \vdash (H', e'): \tau$

Translation validation for secret independence

CLASSIFY $\mathcal{C} \vdash i : \pi$	BINOPPUB o is constant-tin	ne	BINOPPRIV <i>o</i> is not constant-time		
$\overline{C \vdash i : \sigma}$	$C \vdash t.binop \ o : m \ m \to m$		$C \vdash t$.binop $o : \pi \pi \to \pi$		
Load		Loca	$C(\ell) = m$		
$\overline{C \vdash t.load} : *\sigma \ \pi \to \sigma$		$C \vdash $	$C \vdash \text{get_local } \ell : [] \rightarrow m$		
	$\frac{C \text{OND}}{C \vdash i_1 : \vec{m} \to \pi}$	$C \vdash \overrightarrow{i_{\{2,3\}}}$	$\vec{a}:\vec{m}\rightarrow\vec{m}$		

Performance evaluation of WHACL*

Primitive (blocksize, #rounds)	HACL*	libsodium	WHACL*
Curve25519 (1k)	0.83 s	0.15 s	4.05 s
Chacha20 (4kB, 100k)	1.86 s	1.74 s	6.62 s
Salsa20 (4kB, 100k)	1.55 s	2.24 s	5.52 s
Ed25519 sign (16kB, 1k)	3.01 s	0.27 s	15.6 s
Ed25519 verify (16kB, 1k)	3.07 s	0.24 s	15.6 s
Poly1305_32 (16kB, 10k)	0.27 s	0.19 s	_
Poly1305_64 (16kB, 10k)	1.93 s	0.19 s	11.5 s
SHA2_256 (16kB, 10k)	1.64 s	1.84 s	3.5 s
SHA2_512 (16kB, 10k)	1.16 s	1.21 s	3.2 s

Application : the Signal protocol



Conclusion

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Adapting the proof from [Pro+17] is the most direct path to improve our confidence in the correctness of the translation to WebAssembly. However, the Trusted Code Base is quite big with the F* compiler and Kremlin. A WebAssembly backend for CompCert could be a significant contribution towards a certified Web-compatible toolchain.

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The Signal case study demonstrate the ability of the F* and Pro/CryptoVerif ecosystem to handle the proof of non-trivial properties (including functional correctness and security) of a large codebase, that can be extracted with a high confidence to portable code.

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